The Foundation of Rigorous Inference: Bayesian Statistics — Syllabus

Unofficial/Short Course Title: Bayesian Statistics

Fall 2024, Deep Springs College, Prof. Brian Hill

Overview

There are two types of inferential statistics that are widely used: frequentist and Bayesian. Frequentist inference is an oversimplification, and it sometimes gives obviously wrong results. However, frequentist inference remains the dominant way that statistics is learned and applied to experimental data to make claims because it is somewhat easier to learn. We will begin with the unassailable basics which underly both frequentist and Bayesian statistics. The basics common to both are known as "descriptive statistics." After covering descriptive statistics, we can spend some time on frequentist inference, including the derivation of the linear regression formulae. Then we will graduate to Bayesian statistics.

Prerequisite / Joining the Class

I will use mathematics that is commonly known as either Algebra 2 or Algebra 3-4. We will need to develop and use some calculus to do statistics, and I will go slowly and assume you have never seen any calculus. If you had calculus in high school, be patient. This class was pitched as the much more accessible complement to the other class I am teaching this semester.

Texts

We are going to use three texts. How much of the third one we get to will depend on our pace in the second one. In order, the three texts we will use are:

- Hugh Young, **Statistical Treatment of Experimental Data** (this is a compact classic that will be of use no matter what additional statistics you do or don't ever use)
- Therese Donovan and Ruth Mickey, **Bayesian Statistics for Beginners** (this is the book we will use the most it is at a good level for our purposes)
- E.T. Jaynes and G. Larry Bretthorst, **Probability Theory: The Logic of Science** (this is pretty advanced, but working hard with the second text will make it accessible)

Grading

- 45% assignments
- 15% (45% total) for each of three exams, dates to be determined, but coming at about the 5th, 9th, and 14th week of classes
- 10% preparation for class and leadership of course

Problem Sets / Handouts / Being Neat and Organized

There will be at least one problem set every week, and ideally more if I can produce one for every class. There will also be handouts, problem set solutions, exams, and exam solutions. To be organized, locate a three-ring binder and a three-ring hole punch, and file everything chronologically. Reverse-chronological is actually the most convenient, because you always open your binder to what you are currently working on. Problem sets should be *neat* and on standard $8 1/2 \times 11$ paper. Multi-page problem sets should be stapled. The nicest technical work is facilitated by engineering pads, such as these **stinking expensive Roaring Spring Engineering Pads at Amazon**, and done with a mechanical pencil, a ruler, and an eraser at hand.

Absences (and late work)

The College's policies on absences (and late work) are applicable. Refer to the Deep Springs Handbook.