Brian Hill Aug. 30, 2022 Numerical Examples for Day 1 Ratios and Speeds 1. An illustration of ratios (à la Euclid Book II, definition 5) Consider four quantities 2V7 rabbits - the first as modern readers we have no travble just saying these are both ratios of J7 Z rabbits - the second (4 JT apples - the third S 4 apples - the fourth How does Euclid say tells us to test, 77 whether these are the same ratio. As a hint, which continues in the spirit of definition 5, consider the equimultiple of the first and third to be UT and the equimultiple of the second and fourth to be 71. Or take the equimultiple of the first and third to again be of, but this time the equimultiple of the second and fourth to be, 3. Bonus consideration for modern readers: what is it the interpretation of the ratio of the third to the first I think Euclid would not want us to consider this!

2. An Application of Galileo's Theorem III, Proposition II A modern For modern readers, we have no trouble Ple reader upon dividing a unit of distance by a unit of time to get a unit of speed or velocity, for example mph = miles I think Galileo, like Euclid, does not want us to consider such mixed encountering the à example below wovid do 3 $\frac{1}{2} = \frac{1}{2} \frac{$ ratios. So let us introduce a new, primitive, and nondecomposable wit inite 60 seconds of speed, the MUFF, so we are not tempted to start using modern and use t= 5 methods in our illustration. Car 1 sets off from Lone Pine to Bishop at 60 muff. Car 2 sets off at 45 muff. What is the ratio of the speed of Car 2 to Car 1 ? Simplify it. what is inverse of this ratio? We observe that Car I gets to the first mile marker in 60 seconds. According to Theorem III, Proposition III, when will we observe Car Z reaching the first mile marker?