

Proposition 10, p. 209

$$\frac{1}{F} \propto \frac{(QT)^2 (CP)^2}{QR}$$

$$= \frac{(QT)^2 (CP)^2}{PV}$$

$$= \frac{(QV)^2 (PF)^2}{PV}$$

$$= \frac{UG (CD)^2 (PF)^2}{(PC)^2}$$

$$= \frac{2 (CD)^2 (PF)^2 \cancel{PC}}{(PC)^2}$$

$$= \frac{2 (BC)^2 (CA)^2}{PC}$$

or simply

$$F \propto PC$$

By I.6 Corollary 1 p. 182

Trivial

Similar triangles

$$\frac{QV}{QT} = \frac{PC}{PF} \quad \text{or} \quad QT \cdot PC = QV \cdot PF$$

From Conics - Apollonius I.21

$$\frac{PV \cdot UG}{(QV)^2} = \frac{(PC)^2}{(CD)^2} \quad \text{or} \quad \frac{(QV)^2}{PV} = UG \frac{(CD)^2}{(PC)^2}$$

$$UG = 2PC \quad \text{in evanescently}$$

$$\text{Lemma 12} \quad CD \cdot PF = BC \cdot CA$$

because (BC) and CA
are given